STUDY MODULE DESCRIPTION FORM				
Name of the module/subject Combinatorial Optimization				Code 1010511331010510332
Field of study			Profile of study	Year /Semester
Computing			(general academic, practical general academic	<sup>I)</sup> 2/3
Elective path/specialty			Subject offered in:	Course (compulsory, elective)
		-	Polish	obligatory
Cycle o	f study:		Form of study (full-time,part-time)	)
First-cycle studies			full-time	
No. of h	ours			No. of credits
Lectu	re: <b>30</b> Classes	s: - Laboratory: 15	Project/seminars:	- 3
Status of the course in the study program (Basic, major, other) (university-wide, from another field)				
major trom field				
Educati	on areas and neids of sch	ence and an		and %)
Responsible for subject / lecturer: Maciej Drozdowski email: Maciej.Drozdowski@cs.put.poznan.pl tel. 616652981 Computer Science				
ul. Piotrowo 2, 60-965 Poznań				
Prerequisites in terms of knowledge, skills and social competencies:				
1	Knowledge	A student beginning this subject of study should have basic understanding of discrete mathematics (set theory, logic, graph theory), methods of algorithm design, basic programming structures, abstract data types (e.g. lists, stacks, queues, arbitrary graphs), typical algorithms (e.g. sorting, search in data structures), also basic knowledge on the computational complexity of algorithms and problems.		
2	Skills	The student should be able to design basic algorithms and code them, to recognize basic discrete structures, to estimate computational complexity of algorithms, as well as acquire information from the indicated sources.		
3	Social competencies	The student should understand the necessity of expanding his/her competences and be ready to undertake cooperation in a team. As far as social competences are considered, the student must be honest, responsible, persevering, curious, creative, respectful to other people.		
Assumptions and objectives of the course:				
Course goals:				
Introdu	iction into basic proble	ms of combinatorial optimization	and the methods of solving the	em. In particular:
<ol> <li>acquiring ground understanding on optimizing problems with discrete nature,</li> <li>demonstrating solvability barrier arising from exponential computational complexity of algorithms and computational</li> </ol>				
hardness of problems and stimulate understanding consequences of this barrier,				
<ol> <li>familiarizing with the methodology of analyzing and practically solving of computationally hard optimization tasks for</li> </ol>				
problems with discrete nature.				
Study outcomes and reference to the educational results for a field of study				
Knowledge:				
1. acquire knowledge on algorithms and their complexity - [K1st_W4]				
2. have particular knowledge on algorithm design - [K1st_W5]				
algorithms and discrete problems - [K1st_W7]				
4. 4. understand consequences of the computational hardness of problems and know practical methods of solving such problems - [-]				
Skills:				

1. 1. design and conduct simple experiments, in particular computer measurements and simulations, analyze obtained results and draw conclusions - [K1st\_U3]

2. apply analytical and experimental methods to solve computer science methods - [K1st\_U4]

3. estimate computational complexity of algorithms and problems - [K1st\_U8]

4. design and code algorithms using at least one popular tool - [K1st\_U11]

## Social competencies:

1. understands that knowledge and skills in computer science quickly change and deprecate - [K1st\_K1]

2. understands the meaning of knwoledge in solving engineering problems, knows examples engineering problems leading to social losses - [K1st\_K2]

## Assessment methods of study outcomes Formative assessment: lectures: a) ? based on answers to question asked and open problems posed during the lectures, b) labs: ? evaluation of the correctness of the programs solving the assigned combinatorial optimization problems ? evaluation of student?s knowledge necessary to prepare, and carry out the lab tasks Total assessment: a) lectures: ? based on answers to question in a written exam, b) labs: ? monitoring students? activities during classes, ? evaluation of reports on the method and computer program solving the assigned combinatorial optimization problems Additional elements cover: 2 punctuality: additional points for providing solutions (programs) and reports on time ? efficiency (time, quality) of the solutions delivered by the student programs ? ability to work in a team solving a lab assignment ? recommendations improving the teaching process

## Course description

The lecture covers the following topics: Pseudopolynomial dynamic programming algorithms for partition and knapsack problems. Strong NP-hardness. Computational complexity of optimization problems: NP-hardness. The notion of approximation algorithms, examples of approximation algorithms. Hardness of approximation. Computationally easy combinatorial optimization problems: Shortest paths in graphs: Dijkstra's algorithm, DAG algorithm, all-pair shortest paths algorithm. Transitive closure of a binary relation: Floyd-Warshall algorithm. Network flows and related problems: maximum flow problem, Dinic algorithm. flows with minimum arc flow, minimum cost flows, matching in a bipartite graph, applications of max flow problem in solving scheduling problems and graph partitioning. Minimum spanning tree: Kruskal and Prim algorithms. The notion of a matroid. Graph coloring problem: formulation, applications, algorithms. Packing and cutting: formulation, applications, bin packing problem, algorithms for bin packing.

During the lab-classes students solve NP-hard combinatorial optimization problems. It is required to design and code at least two algorithms solving the assigned problem: a fast method (e.g. greedy algorithm) and of improved quality solutions method (e.g. a branch and bound or metaheuristic method).

## **Basic bibliography:** 1. Złożoność obliczeniowa problemów kombinatorycznych, J. Błażewicz, WNT, W-wa, 1988 2. Scheduling Computer and Manufacturing Processes, J. Błażewicz, K. Ecker, E.Pesch, G. Schmidt, J. Weglarz, Springer, Berlin, New York, 2001 3. Kombinatoryka dla programistów, W. Lipski , WNT, W-wa, 1982 4. Computers and intractability: A guide to the theory of NP-completeness, M.R.Garey, D.S.Johnson, W.H.Freeman, San Francisco, 1979 5. Combinatorial optimization, W.Cook, W.Cunningham, W.Pullevblank, A.Schrijver, Wiley & Sons, 1998 6. Algorytmy optymalizacji dyskretnej z programami w języku Pascal, M.Sysło, N.Deo, J.Kowalik, PWN, Warszawa, 1993 7. Wprowadzenie do algorytmów, T.Cormen, C.Leiserson, R.Rivest, C.Stein, WNT, Warszawa, 2005 8. Optymalizacja dyskretna modele i metody kolorowania grafów, pod red. M.Kubale, WNT, Warszawa, 2003. 9. Złożoność obliczeniowa problemów kombinatorycznych, J. Błażewicz, WNT, W-wa, 1988 10. Scheduling Computer and Manufacturing Processes, J. Błażewicz, K. Ecker, E.Pesch, G. Schmidt, J. Weglarz, Springer, Berlin, New York, 2001 11. Kombinatoryka dla programistów, W. Lipski , WNT, W-wa, 1982 12. Computers and intractability: A guide to the theory of NP-completeness, M.R.Garey, D.S.Johnson, W.H.Freeman, San Francisco, 1979 13. Combinatorial optimization, W.Cook, W.Cunningham, W.Pulleyblank, A.Schrijver, Wiley & Sons, 1998 14. Algorytmy optymalizacji dyskretnej z programami w języku Pascal, M.Sysło, N.Deo, J.Kowalik, PWN, Warszawa, 1993 15. Wprowadzenie do algorytmów, T.Cormen, C.Leiserson, R.Rivest, C.Stein, WNT, Warszawa, 2005 16. Optymalizacja dyskretna modele i metody kolorowania grafów, pod red. M.Kubale, WNT, Warszawa, 2003. Additional bibliography: 1. M.Drozdowski, D.Kowalski, J.Mizgajski, D.Mokwa, G.Pawlak, Mind the gap: a heuristic study of subway tours, Journal of Heuristics vol.20, Issue 5, October 2014, pp 561-587, DOI 10.1007/s10732-014-9252-3 2. Jakub Marszałkowski, D.Mokwa, M.Drozdowski, Ł.Rusiecki, H.Narożny, Fast algorithms for online construction of web tag clouds, Engineering Applications of Artificial Intelligence, vol. 64 (2017) pp. 378-390 DOI: 10.1016/j.engappai.2017.06.023 Result of average student's workload Time (working Activity hours) 1. participating in laboratory classes: 15hours 15 2. finalizing lab reports (student's own work in the off lab hours) 5 3. coding, running, verifying, and testing performance of the algorithms (student's own work in the off 10 lab hours) 30 4. attending lectures 10 5. reading and learning from the indicated literature and other sources (approx. 10 pages per hour), 10 approx.100 pages 6. learning for the final exam, and writing the exam Student's workload Source of workload hours **ECTS** 3 Total workload 80 45 2 Contact hours

Practical activities

30

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